

Package ‘nvctr’

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Type Package

Title The n-vector Approach to Geographical Position Calculations using an Ellipsoidal Model of Earth

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Description The n-vector framework uses the normal vector to the Earth ellipsoid (called n-vector) as a non-singular position representation that turns out to be very convenient for practical position calculations. The n-vector is simple to use and gives exact answers for all global positions, and all distances, for both ellipsoidal and spherical Earth models. This package is a translation of the 'Matlab' library from FFI, the Norwegian Defence Research Establishment, as described in Gade (2010) <doi:10.1017/S0373463309990415>.

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URL <https://nvctr.ansperformance.eu>,
<https://github.com/euctrl-pru/nvctr>

BugReports <https://github.com/euctrl-pru/nvctr/issues>

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along_track_distance *Compute the along-track distance from a great circle arc*

Description

Compute the along-track distances of a body, ‘b’ (for example a ground level projection position of an aircraft), from two geographical coordinates, ‘a1’ and ‘a2’ (for example an airport’s runway thresholds), of a great circle arc.

Usage

along_track_distance(b, a1, a2)

Arguments

b	the geographical coordinates (WGS84) of a body: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)
a1	the geographical coordinates (WGS84) of one end of a great circle arc: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)

a2 the geographical coordinates (WGS84) of the other end of a great circle arc: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)

Value

the surface along-track distances from 'b's cross-track intersection to 'a1' - 'a2'

See Also

Other utilities: [altitude_azimuth_distance\(\)](#), [cross_track_distance\(\)](#), [cross_track_intersection\(\)](#)

Examples

```
## Not run:
b <- c(8.086135, 49.973942, 6401)
# EDDF: 07R (longitude, latitude, altitude)
a1 <- c(8.53417, 50.0275, 328)
# EDDF: 25L
a2 <- c(8.58653, 50.0401, 362)
along_track_distance(b, a1, a2)

## End(Not run)
```

altitude_azimuth_distance

Calculate the altitude, azimuth and distance of B from A

Description

The altitude (elevation from the horizon), azimuth and distance of a point B from A are the coordinates of the Topocentric Coordinate System as typically used in astronomy to aim your telescope to a heavenly body. It can be also of use to know where an airplane is in the sky with respect to an observer on Earth.

Usage

```
altitude_azimuth_distance(a, b)
```

Arguments

a the observer position: a vector of longitude, latitude (in decimal degrees) and altitude (in meters) in WGS84

b the observed position: a vector of longitude, latitude (in decimal degrees) and altitude (in meters) in WGS84

Value

the coordinates in North-East-Up of the observed, B, with respect to the observer A. A vector of **altitude** (elevation from the horizon) in decimal degrees, **azimuth** in decimal degrees and distance in meters.

See Also

Other utilities: [along_track_distance\(\)](#), [cross_track_distance\(\)](#), [cross_track_intersection\(\)](#)

Examples

```
## Not run:
# sensor (longitude, latitude, altitude)
a <- c(49.47, 7.697, 274)
# aircraft (longitude, latitude, altitude)
b <- c(49.52, 7.803, 6401)
altitude_azimuth_distance(a, b)

## End(Not run)
```

cross_track_distance *Compute the cross-track distance from a great circle arc*

Description

Compute the cross-track distance of a body, 'b' (for example a ground level projection position of an aircraft), from a great circle arc determined by two geographical coordinates, 'a1' and 'a2' (for example an airport's runway thresholds).

Usage

```
cross_track_distance(b, a1, a2)
```

Arguments

b	the geographical coordinates (WGS84) of a body: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)
a1	the geographical coordinates (WGS84) of one end of a great circle arc: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)
a2	the geographical coordinates (WGS84) of the other end of a great circle arc: a vector of longitude, latitude (in decimal degrees) and eventually altitude (in meters)

Value

the surface cross-track distance from 'b' to the arc 'a1' - 'a2'

See Also

Other utilities: [along_track_distance\(\)](#), [altitude_azimuth_distance\(\)](#), [cross_track_intersection\(\)](#)

Examples

```
## Not run:
b <- c(8.086135, 49.973942, 6401)
# EDDF: 07R (longitude, latitude, altitude)
a1 <- c(8.53417, 50.0275, 328)
# EDDF: 25L
a2 <- c(8.58653, 50.0401, 362)
cross_track_distance(b, a1, a2)

## End(Not run)
```

cross_track_intersection

Calculate cross-track intersection

Description

Calculate the cross-track intersection between the position of a body (i.e. an aircraft) and a great circle arc as defined by two points (i.e. the runway's thresholds).

Usage

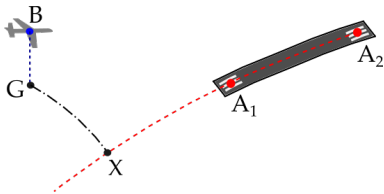
```
cross_track_intersection(b, a1, a2)
```

Arguments

b	coordinates of the body, b: a vector of longitude, latitude (in decimal degrees) and altitude (in meters) in WGS84
a1	first coordinate of a great circle arc: a vector of longitude, latitude (in decimal degrees) and elevation (in meters) in WGS84
a2	second coordinate of a great circle arc: a vector of longitude, latitude (in decimal degrees) and elevation (in meters) in WGS84

Details

The cross-track intersection between the position of a body, B, (i.e. an aircraft) and a great circle arc as defined by two points, A1 and A2, (i.e. the runway's thresholds) is the intersection, X, of the above arc with the great circle arc passing through the ground projection of B, G, and perpendicular to A1-A2.



Value

a WGS84 vector with longitude and latitude (decimal degrees)

See Also

Other utilities: [along_track_distance\(\)](#), [altitude_azimuth_distance\(\)](#), [cross_track_distance\(\)](#)

Examples

```
## Not run:  
# aircraft (longitude, latitude, altitude)  
b <- c(8.086135, 49.973942, 6401)  
# EDDF: 07R (longitude, latitude, altitude)  
a1 <- c(8.53417, 50.0275, 328)  
# EDDF: 25L  
a2 <- c(8.58653, 50.0401, 362)  
cross_track_intersection(b, a1, a2)  
  
## End(Not run)
```

deg

Convert angle in radians to degrees

Description

Convert angle in radians to degrees

Usage

```
deg(radians)
```

Arguments

radians angle in radians.

Value

angle in degrees.

See Also

[rad](#).

Other helpers: [rad\(\)](#), [unit\(\)](#)

Examples

```
deg(pi/2)
```

lat_lon2n_E	Convert (geodetic) latitude and longitude to n-vector
-------------	---

Description

Convert (geodetic) latitude and longitude to n-vector

Usage

```
lat_lon2n_E(latitude, longitude)
```

Arguments

latitude	Geodetic latitude (rad)
longitude	Geodetic longitude (rad)

Value

n-vector decomposed in E (3x1 vector) (no unit)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_E2lat_lon](#).

Examples

```
lat_lon2n_E(rad(1), rad(2))
```

nvctr	<i>nvctr: non-singular geographical position calculations</i>
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Description

nvctr provides functions to calculate geographical positions for both the ellipsoidal and spherical Earth models.

Author(s)

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Other contributors:

- EUROCONTROL [copyright holder, funder]

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

Useful links:

- <https://nvctr.ansperformance.eu>
- <https://github.com/euctrl-pru/nvctr>
- Report bugs at <https://github.com/euctrl-pru/nvctr/issues>

n_E2lat_lon

Convert n-vector to latitude and longitude

Description

Convert n-vector to latitude and longitude

Usage

n_E2lat_lon(n_E)

Arguments

n_E n-vector decomposed in E (3x1 vector) (no unit)

Value

A vector of geodetic latitude and longitude (rad)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[lat_lon2n_E](#).

Examples

n_E2lat_lon(c(1, 0, 0))

n_E2R_EN

Find the rotation matrix R_EN from n-vector

Description

Find the rotation matrix R_EN from n-vector

Usage

n_E2R_EN(n_E)

Arguments

n_E n-vector decomposed in E (3x1 vector) (no unit)

Value

The resulting rotation matrix (direction cosine matrix) (no unit)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[R_EN2n_E, n_E_and_wa2R_EL](#) and [R_EL2n_E](#).

Examples

n_E2R_EN(c(1, 0, 0))

n_EA_E_and_n_EB_E2p_AB_E

Find the delta position from two positions A and B

Description

Given the n-vectors for positions A (n_EA_E) and B (n_EB_E), the output is the delta vector from A to B (p_AB_E).

Usage

```
n_EA_E_and_n_EB_E2p_AB_E(
  n_EA_E,
  n_EB_E,
  z_EA = 0,
  z_EB = 0,
  a = 6378137,
  f = 1/298.257223563
)
```

Arguments

<code>n_EA_E</code>	n-vector of position A, decomposed in E (3x1 vector) (no unit)
<code>n_EB_E</code>	n-vector of position B, decomposed in E (3x1 vector) (no unit)
<code>z_EA</code>	Depth of system A, relative to the ellipsoid (<code>z_EA = -height</code>) (m, default 0)
<code>z_EB</code>	Depth of system B, relative to the ellipsoid (<code>z_EB = -height</code>) (m, default 0)
<code>a</code>	Semi-major axis of the Earth ellipsoid (m, default [WGS-84] 6378137)
<code>f</code>	Flattening of the Earth ellipsoid (no unit, default [WGS-84] 1/298.257223563)

Details

The calculation is exact, taking the ellipticity of the Earth into account. It is also nonsingular as both n-vector and p-vector are nonsingular (except for the center of the Earth). The default ellipsoid model used is WGS-84, but other ellipsoids (or spheres) might be specified via the optional parameters `a` and `f`.

Value

Position vector from A to B, decomposed in E (3x1 vector)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_EA_E_and_p_AB_E2n_EB_E](#), [p_EB_E2n_EB_E](#) and [n_EB_E2p_EB_E](#)

Examples

```
lat_EA <- rad(1); lon_EA <- rad(2); z_EA <- 3
lat_EB <- rad(4); lon_EB <- rad(5); z_EB <- 6

n_EA_E <- lat_lon2n_E(lat_EA, lon_EA)
n_EB_E <- lat_lon2n_E(lat_EB, lon_EB)

n_EA_E_and_n_EB_E2p_AB_E(n_EA_E, n_EB_E, z_EA, z_EB)
```

 n_EA_E_and_p_AB_E2n_EB_E

Find position B from position A and delta

Description

Given the n-vector for position A (n_EA_E) and the position-vector from position A to position B (p_AB_E), the output is the n-vector of position B (n_EB_E) and depth of B (z_EB).

Usage

```
n_EA_E_and_p_AB_E2n_EB_E(
  n_EA_E,
  p_AB_E,
  z_EA = 0,
  a = 6378137,
  f = 1/298.257223563
)
```

Arguments

n_EA_E	n-vector of position A, decomposed in E (3x1 vector) (no unit)
p_AB_E	Position vector from A to B, decomposed in E (3x1 vector) (m)
z_EA	Depth of system A, relative to the ellipsoid (z_EA = -height) (m, default 0)
a	Semi-major axis of the Earth ellipsoid (m, default [WGS-84] 6378137)
f	Flattening of the Earth ellipsoid (no unit, default [WGS-84] 1/298.257223563)

Details

The calculation is exact, taking the ellipticity of the Earth into account.

It is also nonsingular as both n-vector and p-vector are nonsingular (except for the center of the Earth). The default ellipsoid model used is WGS-84, but other ellipsoids (or spheres) might be specified.

Value

a list with n-vector of position B, decomposed in E (3x1 vector) (no unit) and the depth of system B, relative to the ellipsoid (z_EB = -height)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_EA_E_and_n_EB_E2p_AB_E](#), [p_AB_E2n_EB_E](#) and [n_EB_E2p_AB_E](#)

Examples

```

p_BC_B <- c(3000, 2000, 100)

# Position and orientation of B is given:
n_EB_E <- unit(c(1,2,3)) # unit to get unit length of vector
z_EB <- -400
R_NB <- zyx2R(rad(10), rad(20), rad(30)) # yaw, pitch, and roll
R_EN <- n_E2R_EN(n_EB_E)
R_EB <- R_EN %*% R_NB

# Decompose the delta vector in E:
p_BC_E <- (R_EB %*% p_BC_B) %>% as.vector() # no transpose of R_EB, since the vector is in B

# Find the position of C, using the functions that goes from one
# position and a delta, to a new position:
(n_EB_E <- n_EA_E_and_p_AB_E2n_EB_E(n_EB_E, p_BC_E, z_EB))

```

*n_EB_E2p_EB_E**Convert n-vector to cartesian position vector in meters*

Description

The function converts the position of B (typically body) relative to E (typically Earth), the n-vector *n_EB_E* to cartesian position vector ("ECEF-vector"), *p_EB_E*, in meters.

Usage

```
n_EB_E2p_EB_E(n_EB_E, z_EB = 0, a = 6378137, f = 1/298.257223563)
```

Arguments

<i>n_EB_E</i>	n-vector of position B, decomposed in E (3x1 vector) (no unit)
<i>z_EB</i>	Depth of system B, relative to the ellipsoid (<i>z_EB</i> = -height) (m, default 0)
<i>a</i>	Semi-major axis of the Earth ellipsoid (m, default [WGS-84] 6378137)
<i>f</i>	Flattening of the Earth ellipsoid (no unit, default [WGS-84] 1/298.257223563)

Details

The calculation is exact, taking the ellipticity of the Earth into account.

It is also nonsingular as both n-vector and p-vector are nonsingular (except for the center of the Earth). The default ellipsoid model used is WGS-84, but other ellipsoids (or spheres) might be specified via the optional parameters *a* and *f*.

Value

Cartesian position vector from E to B, decomposed in E (3x1 vector) (m)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[p_EB_E2n_EB_E](#), [n_EA_E_and_p_AB_E2n_EB_E](#) and [n_EA_E_and_n_EB_E2p_AB_E](#).

Examples

```
n_EB_E <- lat_lon2n_E(rad(1), rad(2))
n_EB_E2p_EB_E(n_EB_E)
```

n_E_and_wa2R_EL	<i>Find R_EL from n-vector and wander azimuth angle</i>
-----------------	---

Description

Calculate the rotation matrix (direction cosine matrix) R_EL using n-vector (n_E) and the wander azimuth angle. When wander_azimuth = 0, we have that N = L (See Table 2 in Gade (2010) for details)

Usage

```
n_E_and_wa2R_EL(n_E, wander_azimuth)
```

Arguments

n_E n-vector decomposed in E (3x1 vector) (no unit)
wander_azimuth The angle between L's x-axis and north, positive about L's z-axis (rad)

Value

The resulting rotation matrix (3x3) (no unit)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[R_EL2n_E](#), [R_EN2n_E](#) and [n_E2R_EN](#).

Examples

```
# Calculates the rotation matrix (direction cosine matrix) R_EL
# using n-vector (n_E) and the wander azimuth angle.
n_E <- c(1, 0, 0)
(R_EL <- n_E_and_wa2R_EL(n_E, wander_azimuth = pi / 2))
```

p_EB_E2n_EB_E *Convert cartesian position vector in meters to n-vector*

Description

The position of B (typically body) relative to E (typically Earth) is given as cartesian position vector p_EB_E, in meters ("ECEF-vector").

Usage

```
p_EB_E2n_EB_E(p_EB_E, a = 6378137, f = 1/298.257223563)
```

Arguments

p_EB_E	Cartesian position vector from E to B, decomposed in E (3x1 vector) (m)
a	Semi-major axis of the Earth ellipsoid (m, default [WGS-84] 6378137)
f	Flattening of the Earth ellipsoid (no unit, default [WGS-84] 1/298.257223563)

Details

The function converts to n-vector, n_EB_E and its depth, z_EB.

The calculation is exact, taking the ellipticity of the Earth into account. It is also nonsingular as both n-vector and p-vector are nonsingular (except for the center of the Earth). The default ellipsoid model used is WGS-84, but other ellipsoids (or spheres) might be specified.

Value

n-vector representation of position B, decomposed in E (3x1 vector) (no unit) and depth of system B relative to the ellipsoid (z_EB = -height)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_EB_E2p_EB_E](#), [n_EA_E_and_p_AB_E2n_EB_E](#) and [n_EA_E_and_n_EB_E2p_AB_E](#)

Examples

```
p_EB_E <- 6371e3 * c(0.9, -1, 1.1)
(n_EB_E <- p_EB_E2n_EB_E(p_EB_E))
```

R2xyz

Find the three rotation angles about new axes in the xyz order from a rotation matrix

Description

The angles (called Euler angles or Tait–Bryan angles) are defined by the following procedure of successive rotations: Given two arbitrary coordinate frames A and B, consider a temporary frame T that initially coincides with A. In order to make T align with B, we first rotate T an angle x about its x -axis (common axis for both A and T). Secondly, T is rotated an angle y about the NEW y -axis of T. Finally, T is rotated an angle z about its NEWEST z -axis. The final orientation of T now coincides with the orientation of B. The signs of the angles are given by the directions of the axes and the right hand rule.

Usage

```
R2xyz(R_AB)
```

Arguments

R_AB a 3x3 rotation matrix (direction cosine matrix) such that the relation between a vector v decomposed in A and B is given by: $v_A = R_AB * v_B$

Value

x,y,z Angles of rotation about new axes (rad)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[xyz2R](#), [R2zyx](#) and [zyx2R](#).

Examples

```
R_AB <- matrix(
  c( 0.9980212 ,  0.05230407, -0.0348995 ,
    -0.05293623,  0.99844556, -0.01744177,
     0.03393297,  0.01925471,  0.99923861),
  nrow = 3, ncol = 3, byrow = TRUE)
R2xyz(R_AB)
```

R2zyx

Find the three angles about new axes in the zyx order from a rotation matrix

Description

The 3 angles z , y , x about new axes (intrinsic) in the order z - y - x are found from the rotation matrix R_{AB} . The angles (called Euler angles or Tait–Bryan angles) are defined by the following procedure of successive rotations:

1. Given two arbitrary coordinate frames A and B , consider a temporary frame T that initially coincides with A . In order to make T align with B , we first rotate T an angle z about its z -axis (common axis for both A and T).
2. Secondly, T is rotated an angle y about the NEW y -axis of T . Finally, T is rotated an angle x about its NEWEST x -axis.
3. The final orientation of T now coincides with the orientation of B .

The signs of the angles are given by the directions of the axes and the right hand rule.

Usage

`R2zyx(R_AB)`

Arguments

`R_AB` a 3x3 rotation matrix (direction cosine matrix) such that the relation between a vector v decomposed in A and B is given by: $v_A = R_{AB} * v_B$

Details

Note that if A is a north-east-down frame and B is a body frame, we have that z =yaw, y =pitch and x =roll.

Value

z,y,x angles of rotation about new axes (rad)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[zyx2R](#), [xyz2R](#) and [R2xyz](#).

Examples

`zyx2R(rad(1), rad(-2), rad(-3))`

rad *Convert angle in degrees to radians.*

Description

Convert angle in degrees to radians.

Usage

```
rad(degrees)
```

Arguments

degrees angle in degrees.

Value

angle in radians

See Also

[deg.](#)

Other helpers: [deg\(\)](#), [unit\(\)](#)

Examples

```
rad(30)
```

R_Ee *Select the axes of the coordinate frame E*

Description

This function returns the axes of the coordinate frame E (Earth-Centered, Earth-Fixed, ECEF).

Usage

```
R_Ee(axes = "e")
```

Arguments

axes	Either 'e' or 'E'
------	-------------------

- 'e': z-axis points to the North Pole along the Earth's rotation axis, x-axis points towards the point where latitude = longitude = 0. This choice is very common in many fields.
- 'E': x-axis points to the North Pole along the Earth's rotation axis, y-axis points towards longitude +90deg (east) and latitude = 0. (the yz-plane coincides with the equatorial plane). This choice of axis ensures that at zero latitude and longitude, frame N (North-East-Down) has the same orientation as frame E. If roll/pitch/yaw are zero, also frame B (forward-starboard-down) has this orientation. In this manner, the axes of frame E is chosen to correspond with the axes of frame N and B. The functions in this library originally used this option.

Details

There are two choices of E-axes that are described in Table 2 in Gade (2010):

- e: z-axis points to the North Pole and x-axis points to the point where latitude = longitude = 0. This choice is very common in many fields.
- E: x-axis points to the North Pole, y-axis points towards longitude +90deg (east) and latitude = 0. This choice of axis directions ensures that at zero latitude and longitude, N (North-East-Down) has the same orientation as E. If roll/pitch/yaw are zero, also B (Body, forward, starboard, down) has this orientation. In this manner, the axes of E is chosen to correspond with the axes of N and B.

Value

rotation matrix defining the axes of the coordinate frame E as described in Table 2 in Gade (2010)

References

Kenneth Gade (2010) [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

Examples

R_Ee()

R_EL2n_E

Find n-vector from the rotation matrix (direction cosine matrix) R_EL

Description

Find n-vector from the rotation matrix (direction cosine matrix) R_EL

Usage

```
R_EL2n_E(R_EL)
```

Arguments

R_EL Rotation matrix (direction cosine matrix) (no unit)

Value

n-vector decomposed in E (3x1 vector) (no unit)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_E2R_EN](#), [R_EL2n_E](#) and [n_E_and_wa2R_EL](#).

Examples

```
R_EL <- matrix(
  c(-1, 0, 0,
    0, 1, 0,
    0, 0, -1),
  nrow = 3, ncol = 3, byrow = TRUE)
R_EL2n_E(R_EL)
```

R_EN2n_E

Find n-vector from R_E

Description

Find n-vector from R_E

Usage

```
R_EN2n_E(R_EN)
```

Arguments

R_EN Rotation matrix (direction cosine matrix) (no unit)

Value

n-vector decomposed in E (3x1 vector) (no unit)

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[n_E2R_EN](#), [R_EL2n_E](#) and [n_E_and_wa2R_EL](#).

Examples

```
R_EN <- matrix(  
  c(-1, 0, 0,  
    0, 1, 0,  
    0, 0, -1),  
  nrow = 3, ncol = 3, byrow = TRUE)  
R_EL2n_E(R_EN)
```

unit

Make input vector unit length, i.e. norm == 1

Description

Make input vector unit length, i.e. norm == 1

Usage

```
unit(vector)
```

Arguments

vector a vector

Value

a unit length vector

See Also

Other helpers: [deg\(\)](#), [rad\(\)](#)

Examples

```
unit(c(1,2,3))
```

 xyz2R

 Create a rotation matrix from 3 angles about new axes in the xyz order.

Description

The rotation matrix R_{AB} is created based on 3 angles x , y and z about new axes (intrinsic) in the order x - y - z . The angles (called Euler angles or Tait-Bryan angles) are defined by the following procedure of successive rotations:

1. Given two arbitrary coordinate frames A and B, consider a temporary frame T that initially coincides with A. In order to make T align with B, we first rotate T an angle x about its x -axis (common axis for both A and T).
2. Secondly, T is rotated an angle y about the NEW y -axis of T.
3. Finally, T is rotated an angle z about its NEWEST z -axis. The final orientation of T now coincides with the orientation of B.

The signs of the angles are given by the directions of the axes and the right hand rule.

Usage

xyz2R(x , y , z)

Arguments

x	Angle of rotation about new x axis (rad)
y	Angle of rotation about new y axis (rad)
z	Angle of rotation about new z axis (rad)

Value

3x3 rotation matrix (direction cosine matrix) such that the relation between a vector v decomposed in A and B is given by: $v_A = R_{AB} * v_B$

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[R2xyz](#), [zyx2R](#) and [R2zyx](#).

Examples

xyz2R(rad(10), rad(20), rad(30))

zyx2R

Create a rotation matrix from 3 angles about new axes in the zyx order.

Description

The rotation matrix R_{AB} is created based on 3 angles z , y and x about new axes (intrinsic) in the order z - y - x . The angles (called Euler angles or Tait–Bryan angles) are defined by the following procedure of successive rotations:

1. Given two arbitrary coordinate frames A and B, consider a temporary frame T that initially coincides with A. In order to make T align with B, we first rotate T an angle z about its z -axis (common axis for both A and T).
2. Secondly, T is rotated an angle y about the NEW y -axis of T.
3. Finally, T is rotated an angle x about its NEWEST x -axis. The final orientation of T now coincides with the orientation of B.

The signs of the angles are given by the directions of the axes and the right hand rule. Note that if A is a north-east-down frame and B is a body frame, we have that z =yaw, y =pitch and x =roll.

Usage

```
zyx2R(z, y, x)
```

Arguments

z	Angle of rotation about new z axis
y	Angle of rotation about new y axis
x	Angle of rotation about new x axis

Value

3x3 rotation matrix R_{AB} (direction cosine matrix) such that the relation between a vector v decomposed in A and B is given by: $v_A = R_{AB} * v_B$

References

Kenneth Gade [A Nonsingular Horizontal Position Representation](#). *The Journal of Navigation*, Volume 63, Issue 03, pp 395-417, July 2010.

See Also

[R2zyx](#), [xyz2R](#) and [R2xyz](#).

Examples

```
zyx2R(rad(30), rad(20), rad(10))
```

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